

Efficient modelling of signalling networks using Integer Linear Programming

Enio Gjerga

Paris, France - July 2017

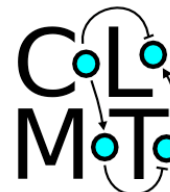
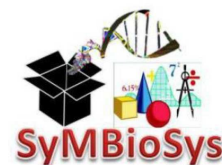


www.saezlab.org

 [@sysbiomed](https://twitter.com/sysbiomed)

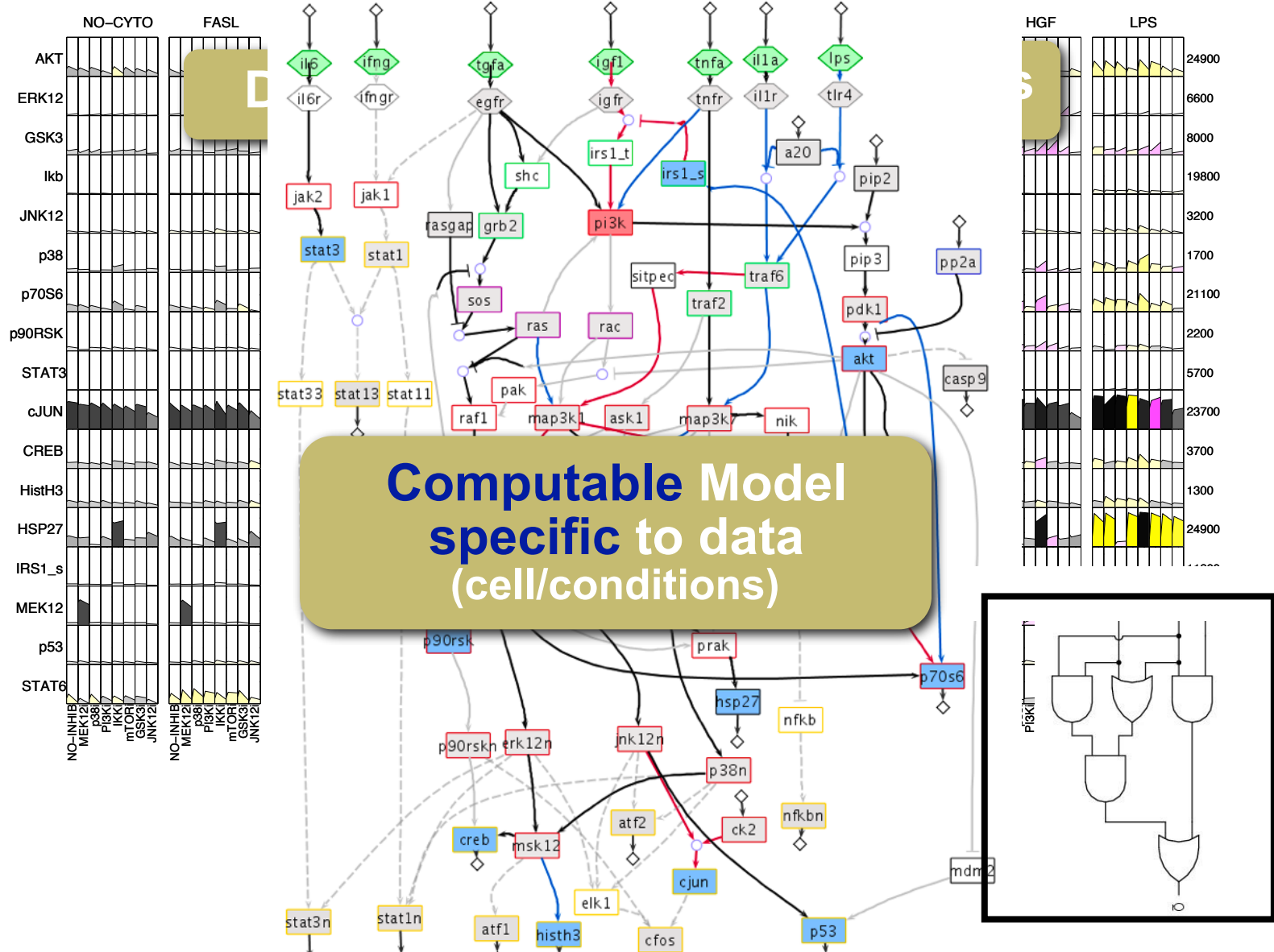


Joint Research Centre for Computational
Biomedicine (JRC-COMBINE)





Logic modeling to link signaling networks with perturbation data



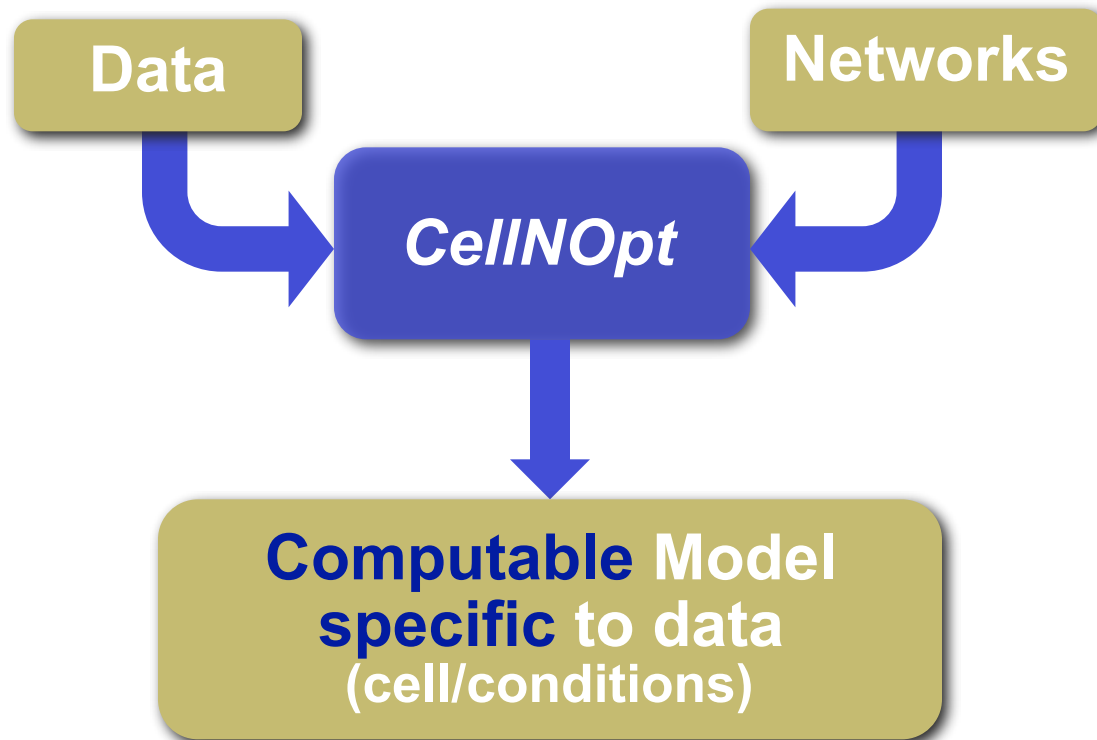
Rodríguez, et al. *Mol. Syst. Biol.*, 2009
Eduati et al. *J Bioinformatics*, 2012

Terfve et al *BMC Sys Bio*, 2012
MacNamara et al. *Phys Biol*, 2012

Terfve et al *Nature Comm*, 2015
Traynard et al., *CPT:PSP*, in press



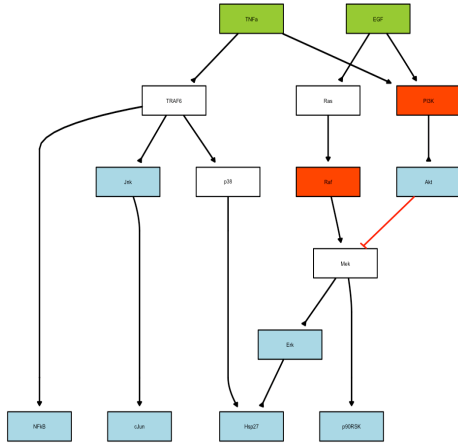
Core task: Optimisation of model against data



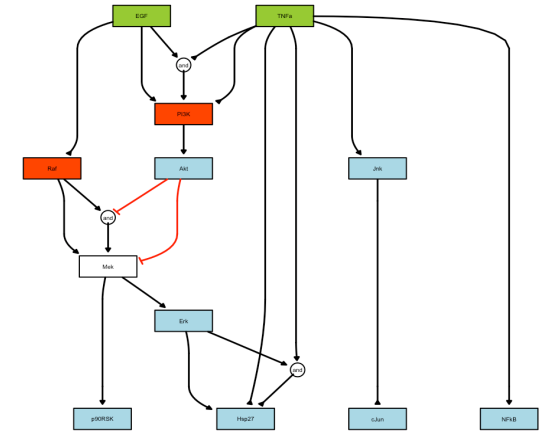


CellNOpt pipeline

Prior Knowledge Network

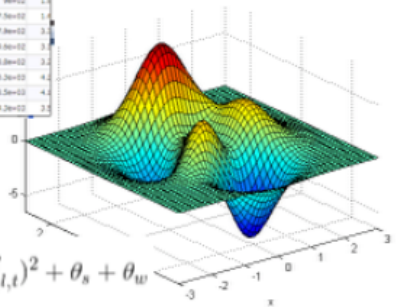


Preprocessing

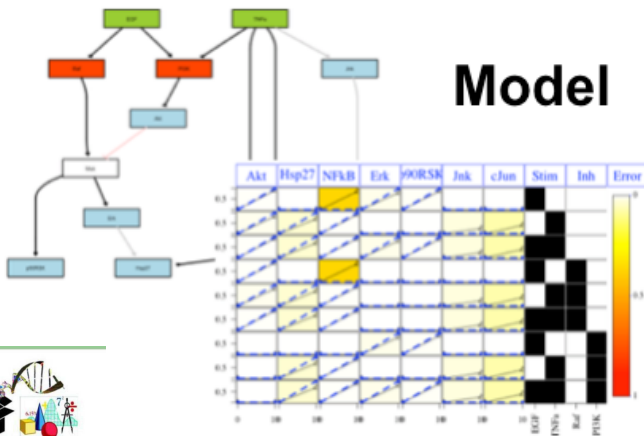


Training

Class	10-HOUR	11:12-ONEP	11-HOUR	11-METS	11:13-ONEP	12-METS
Brain_1_003_00	Brain	5e+02	3.3e+02	4.7e+02	6.8e+04	5.4e+02
Brain_2_004_00	Brain	4e+02	1.2e+02	5.4e+02	6.4e+04	9e+02
Brain_3_005_00	Brain	3.3e+02	4.4e+02	2.8e+02	6.2e+04	5.5e+02
Liver_1_006_00	Liver	2e+02	4.8e+02	1.8e+02	3.2e+02	4.2e+04
Liver_2_007_00	Liver	3.4e+02	4.3e+02	3.3e+02	2.8e+02	4.2e+04
Liver_3_008_00	Liver	3.5e+02	6.2e+02	6.7e+02	3.4e+02	4.2e+04
Spleen_1_009_00	Spleen	6.4e+02	4.7e+02	2.8e+02	6.2e+02	5.2e+04
Spleen_2_010_00	Spleen	6.6e+02	3.3e+02	3.3e+02	6.4e+02	3.5e+04
Spleen_3_011_00	Spleen	7.3e+02	62	7.2e+02	7.5e+02	6.7e+02



Model

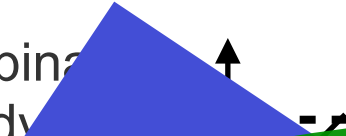


$$\theta_f(P) = \frac{1}{n_g} \sum_{k=1}^s \sum_{l=1}^m \sum_{t=1}^n (B_{k,l,t}^M - B_{k,l,t}^E)^2 + \theta_s + \theta_w$$

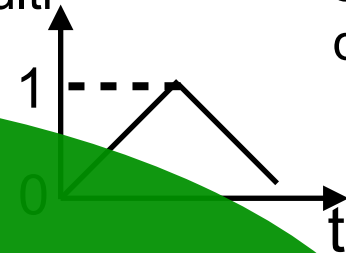


From Boolean to continuous and dynamic models within CellNOpt

Boolean (binary logic steady state)



Boolean multi time-scale

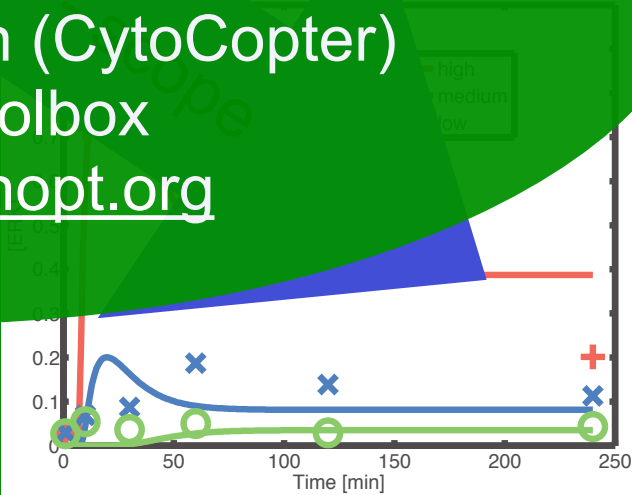
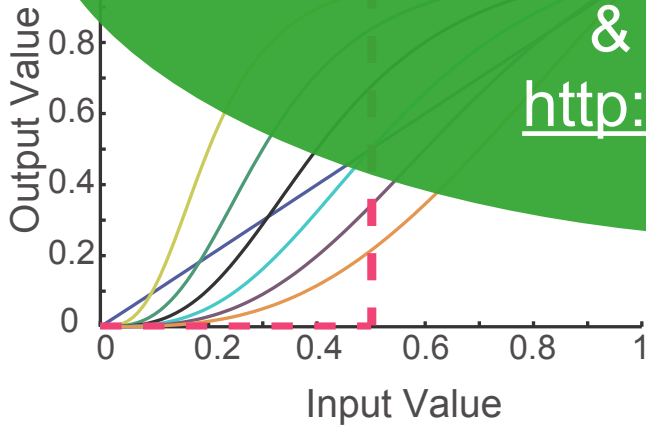


sync. dynamics

Aidan MacNamar

CellNOpt

R/Bioconductor packages (+Python-wrapper) & Cytoscape plug-in (CytoCopter) & Matlab toolbox
<http://www.cellnopt.org>



Wittmann et al. BMC Sys Bio 2009

w. J Banga & J. Egea, B. Penalver

David Henriques

Wittmann et al., PloS Comp Bio 2011





Data

Code	Description	handled in CellNOptR
ID	identifiers	
TR	treatment	yes
DA	Data acquisition	yes
DV	Data value	yes

MIDAS
Minimum Information
for Data Analysis in
Systems Biology

CSV format file containing the cues, signals and readouts

Inhibitors are coded by adding the letter *i* after the name

TR:mock:CellLine	TR:EGF	TR:TNFa	TR:PI3Ki	DA:Akt	DA:Hsp27	DV:Akt	DV:Hsp27
1	1	0	0	0	0	0	0
1	0	1	0	0	0	0	0
1	1	0	0	10	10	1	0.2
1	0	1	0	10	10	1	0.5

Saez-Rodriguez et.al. *Bioinformatics* 2007

Prior Knowledge Network

```
nodeA relationship nodeB
nodeC relationship nodeA
nodeD relationship nodeE nodeF nodeB
```

SBMLqual data format can also be used to load a model

Chaouiya et.al., *BMC Sys Biol*, 2013

SIF - Simple Interaction Format

Cytoscape compatible

relationship can be 1 or -1 (for inhibition)

Simple, but no layout information included



Omnipath: Integration of existing pathway resources to improve modelling

P

www.omnipathdb.org

Networks

Structure & Mechanism

ComPPI
Gene Ontology



Subcellular localization (2)

3DComplexes
3DID
Instruct
Interactome3D



Domains and 3D structures (4)

dbPTM
ELM
HPRD
LMPID
MIMP
Phospho.ELM
PhosphoNetw.
PhosphoSite
Signor



Post-translational modifications (9)

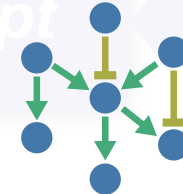
3DComplexes
CORUM
Havugimana



Protein complexes (3)

Unified network of pathways with annotations

OmniPath & pypath



Tissue patterns



Expression

GIANT
HPA
HPM
Prot.DB



Mutations

GDSC

Protein-protein interaction resources (34)

Activity flow (12)

ARN⁺
CA1⁺
CancerCellMap*
DeathDomain
Guide2Pharma⁺
Macrophage⁺
NRF2ome⁺
PDZbase*
Signalink3⁺
Signor⁺
SPIKE⁺
TRIP⁺

Enzyme-substrate (8)

dbPTM*
DEPOD*
DOMINO
ELM
HPRD-phos*
LMPID
phospho.ELM*
PhosphoSite*

Undirected PPI (8)

BioGRID
DIP
HPRD
InnateDB
IntAct
MatrixDB
MPPI
Vidal HI-III

Process description (6)

ACSN
NCI-PID
NetPath

PANTHER
Reactome
WikiPathways

Intervention



Compound target binding

ChEMBL
LINCS
UniChem

Function



GSEA

GO
MSigDB

Gene Ontology



Data

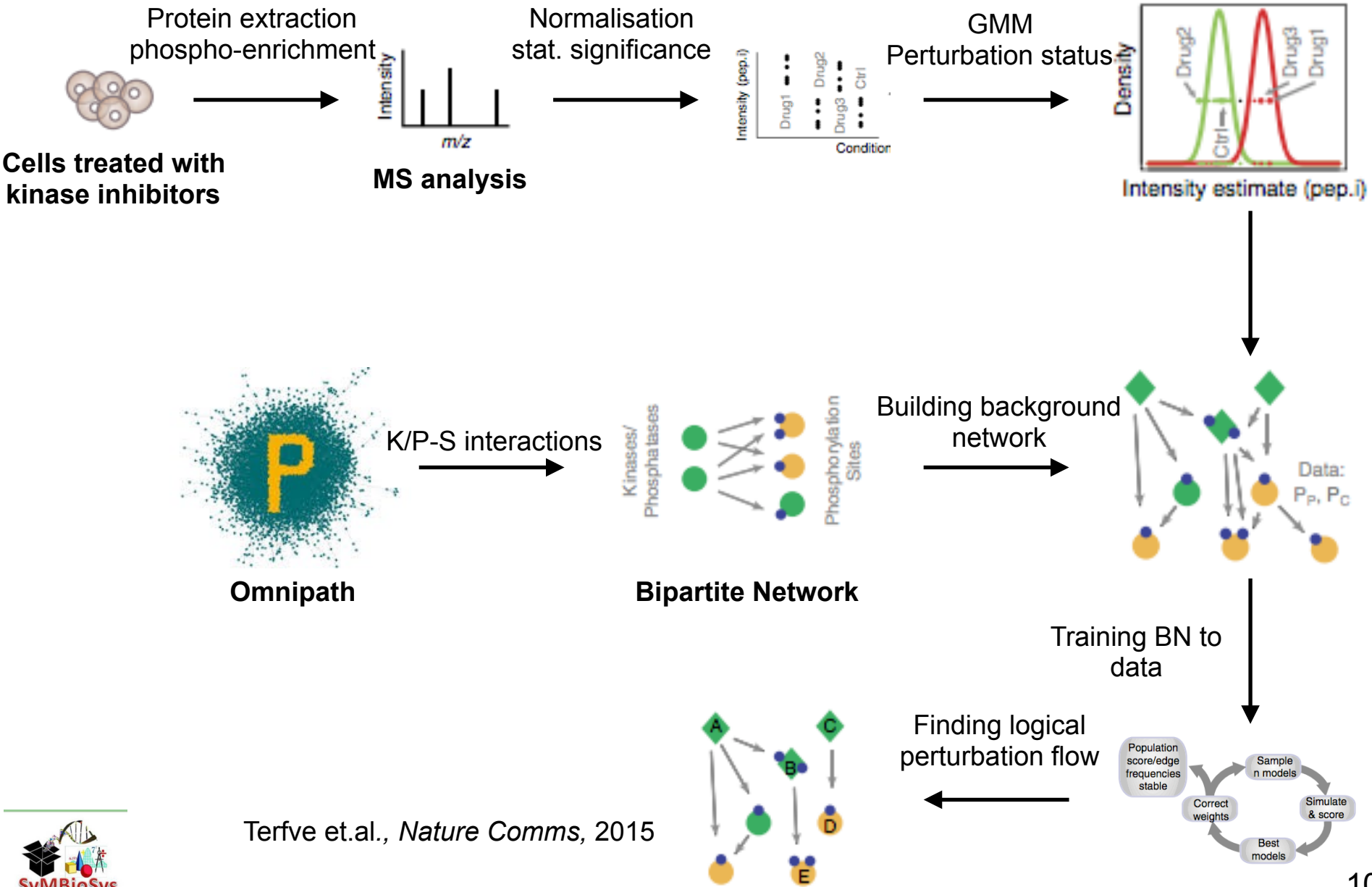
Networks

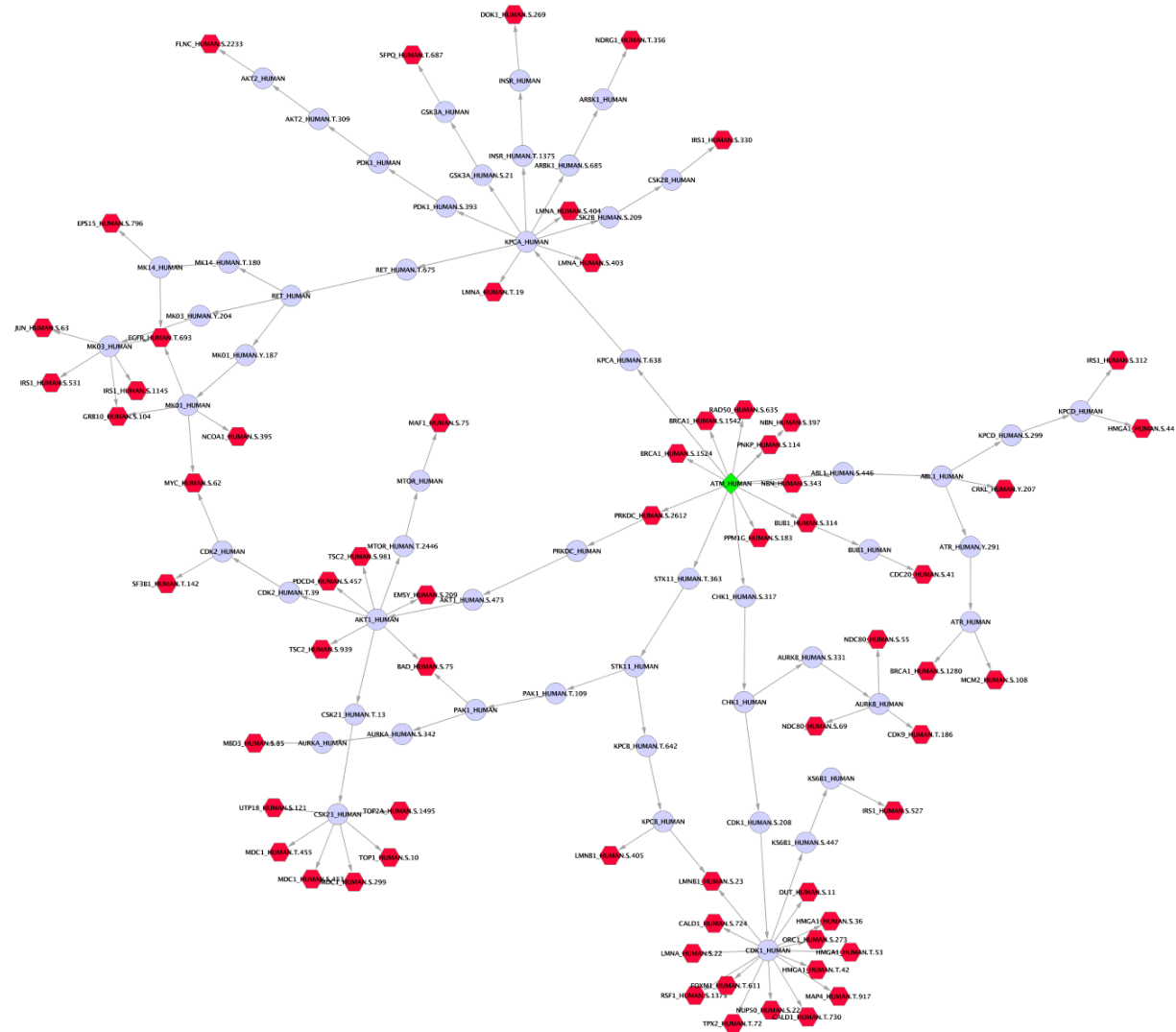
- Antibody-based population data (protein arrays, luminex, ...)
- **Single cell**
- **Mass spectrometry** phospho-proteomics
 - Limited conditions & replicates
- **Metabolic regulation**

Computable Model
specific to data
(cell/conditions)



Using incomplete & noisy mass spectrometry data to build logic models of signal transduction

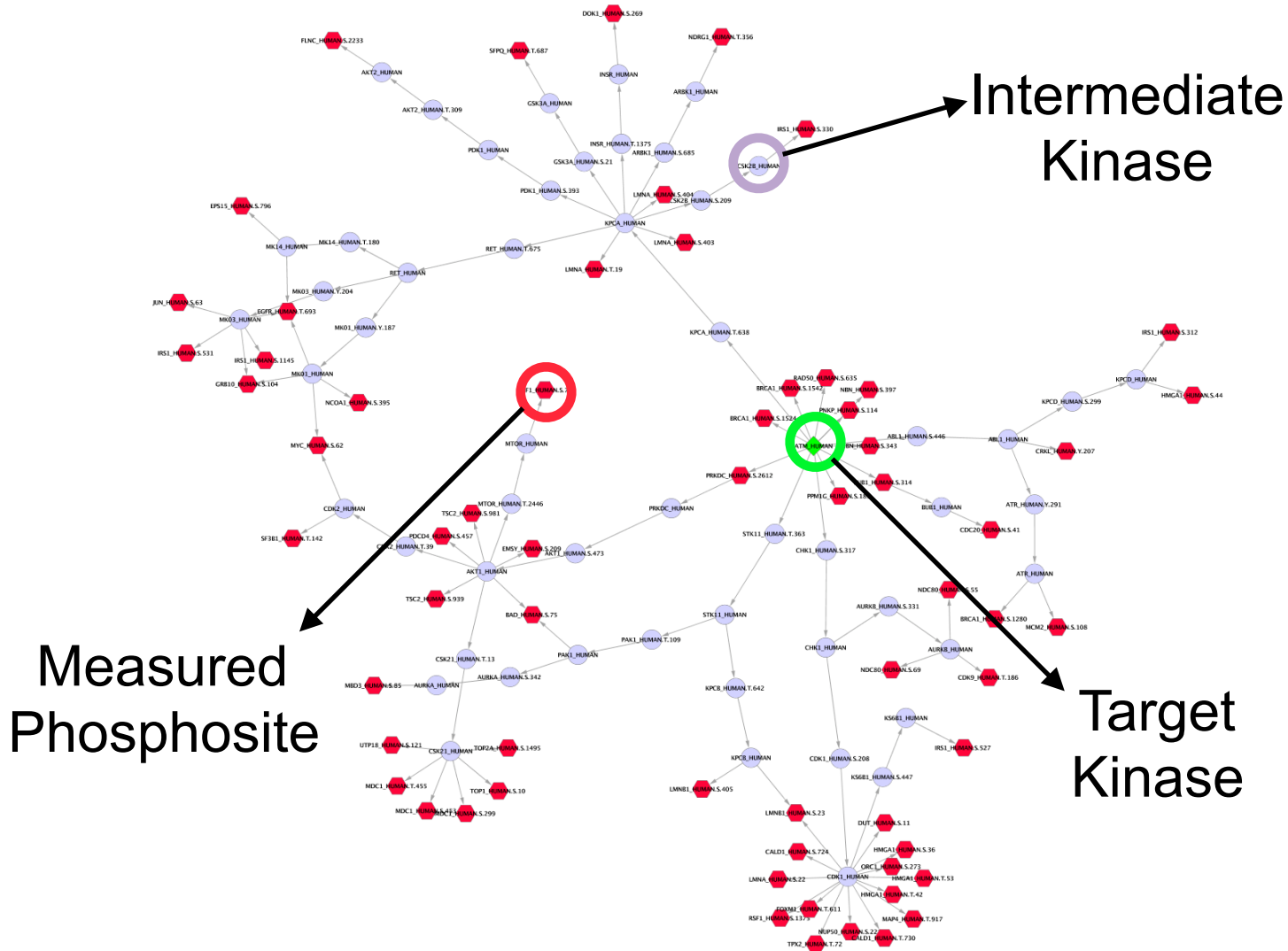




E. Gjerga



PHONEMeS

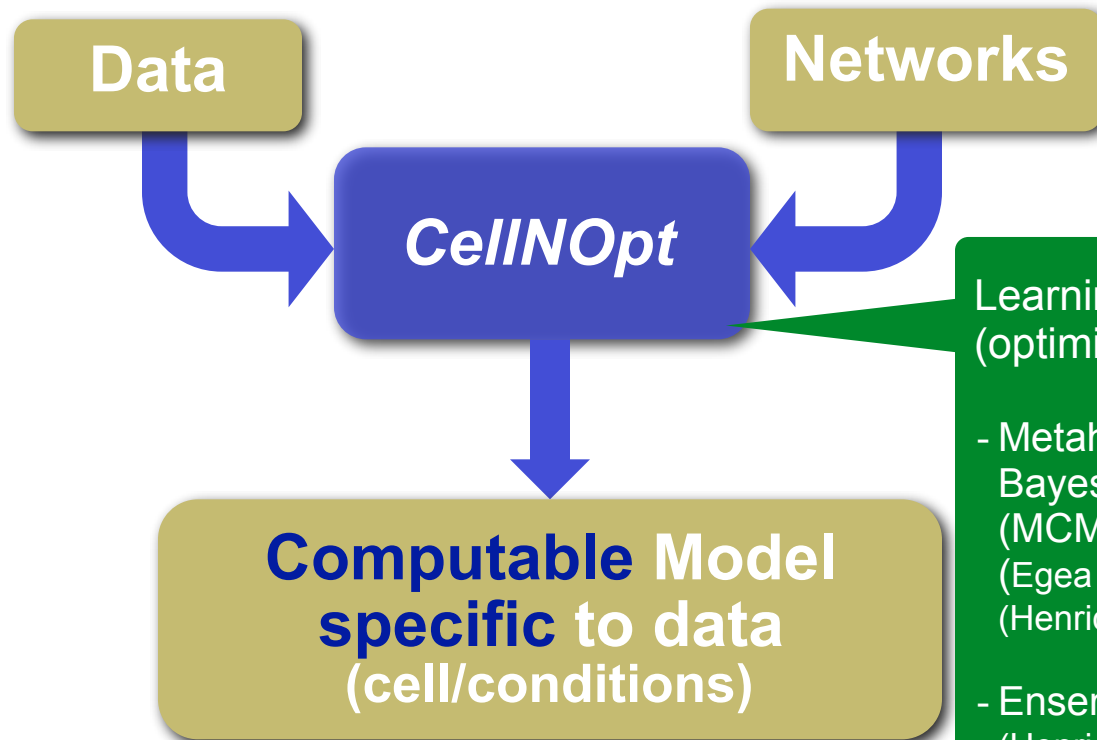


Measured
Phosphosite

Intermediate
Kinase

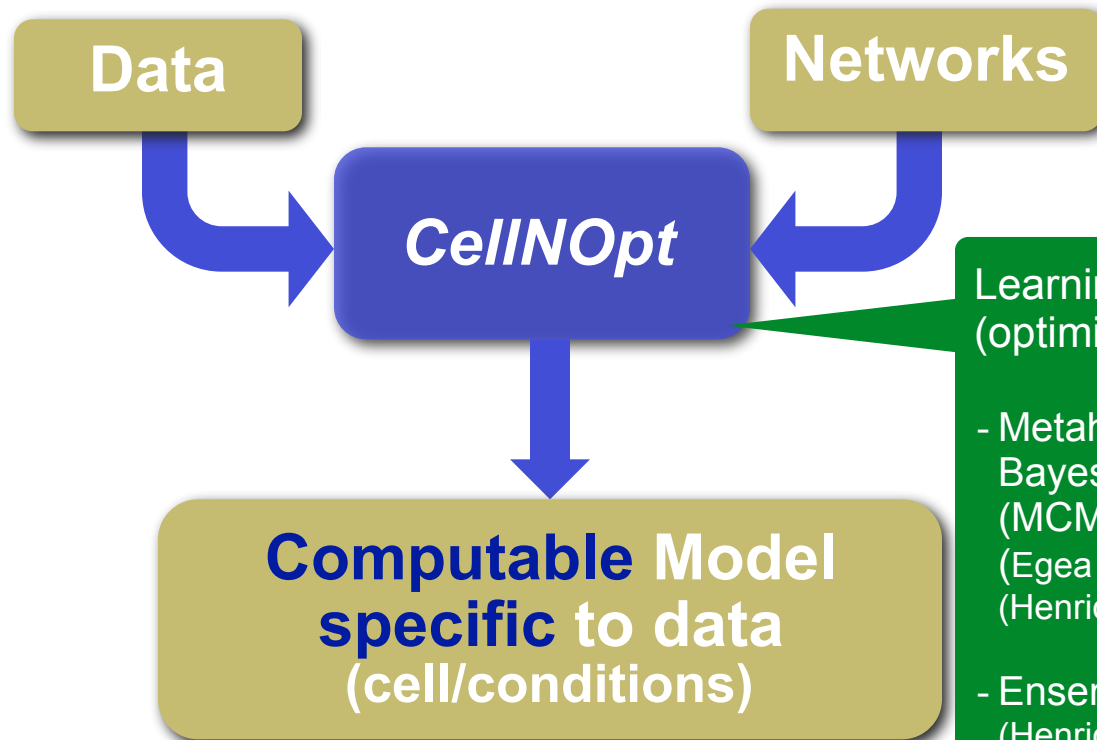
Target
Kinase

E. Gjerga
J. Wirbel



Learning algorithms (optimization):

- Metaheuristics & Bayesian Inference (MCMC) (Egea et al. *BMC Bioinf* 2014; (Henriques et al. *Bioinf* 2015)
- Ensembles of models (Henriques et al. *PLoS CB*, 2017)
- Use of Answer Set Programming (Guziolowski et al. *Bioinf* 2013, Videla et al. *Bioinf* 2017) and Integer Linear Programming (Mitsos et al *PLoS CB* 2009)



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ILP is a mathematical optimisation problem in which the objective function and constraints are linear while the variables are integers

General ILP statement:
$$\min_x (c^T x) \quad s.t.: Ax \leq b, \quad x \in \mathbb{Z}^n$$

Problems with binary decision variables occur often in many signalling model formulations

ILP implementations for **CellNOpt** and **PHONEMeS**

CPLEX solver

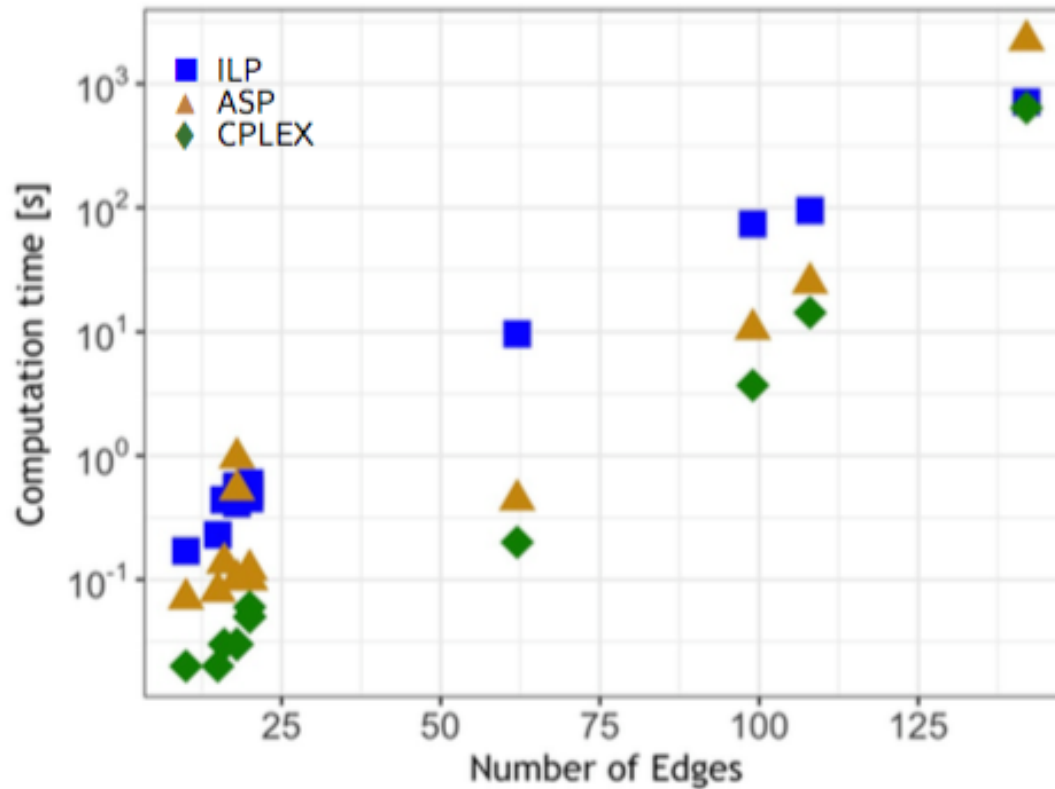




ILP implementation of CellNOpt

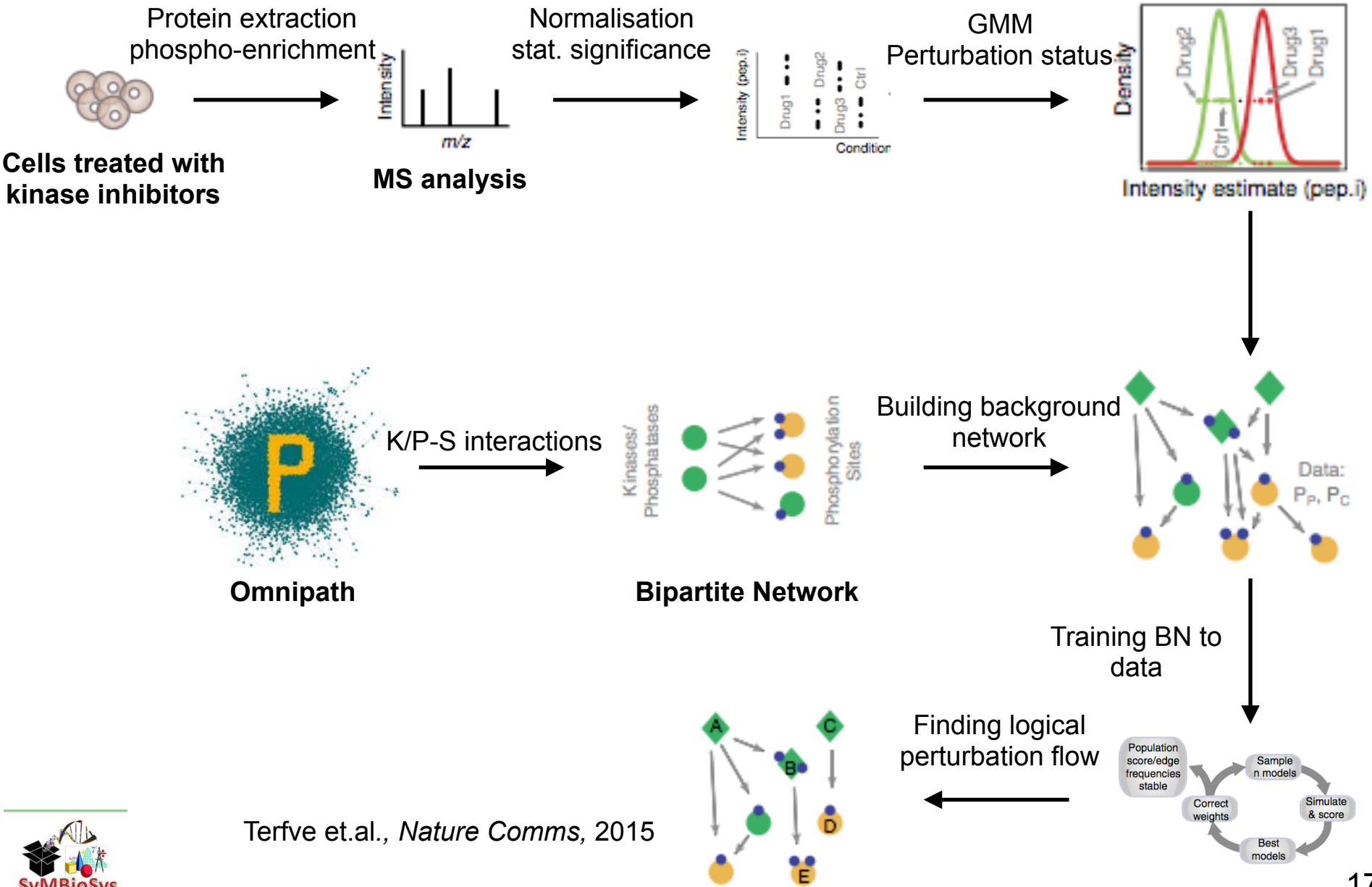
ILP implementation for CellNOpt (*Mitsos et.al.*)

Comparisons between different algorithms applied



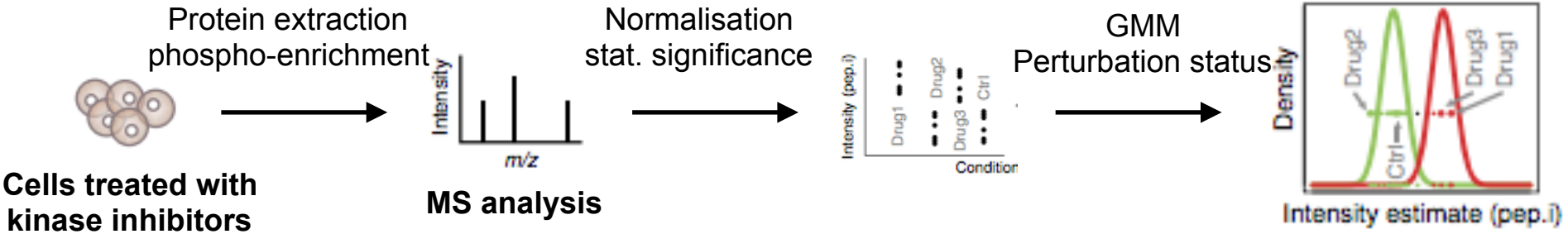


Accelerating model building from mass spectrometry data with ILP





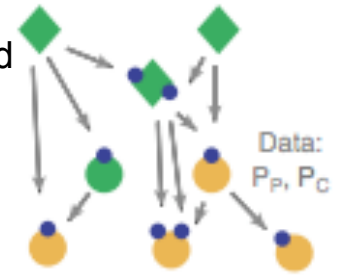
Accelerating model building from mass spectrometry data with ILP



K/P-S interactions



Building background network



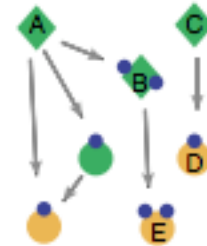
Training BN to data

ILP for PHONEMeS

Can we make it faster??



Finding logical perturbation flow



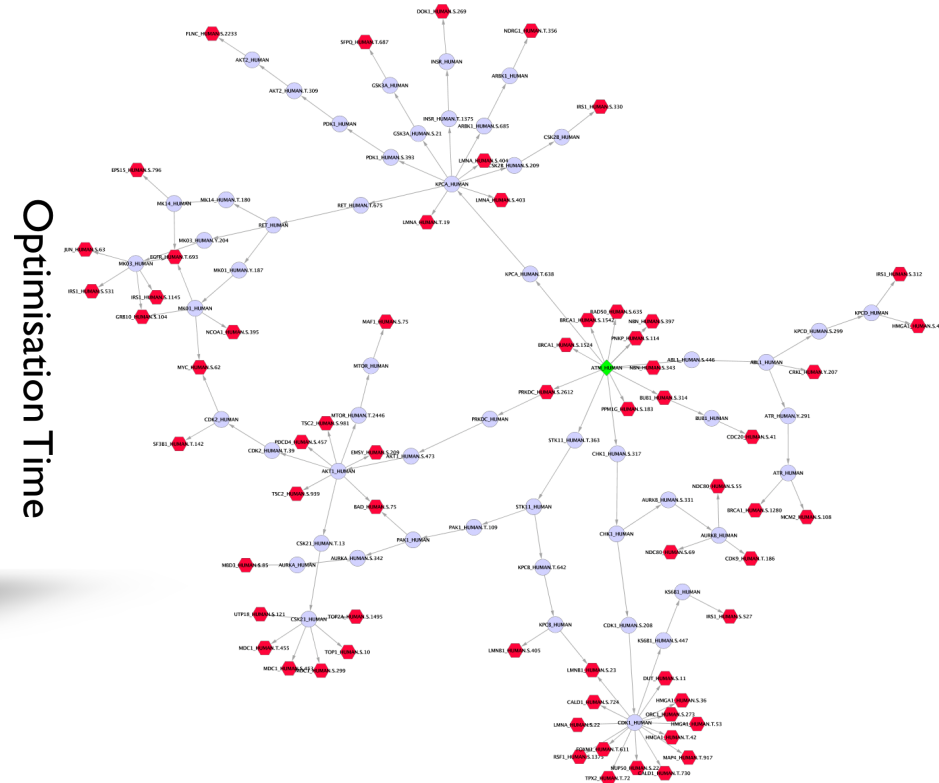
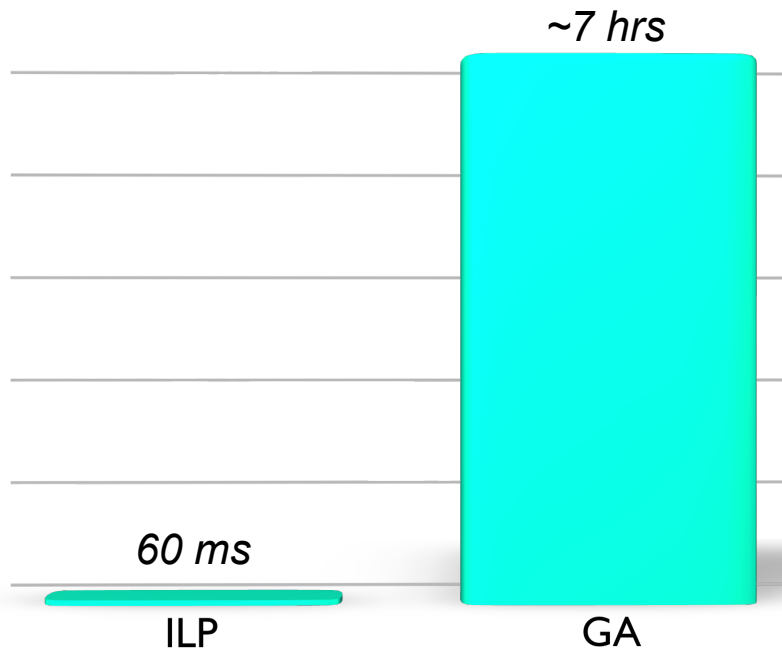
E. Gjerga





Massive speed up with ILP

PHONEMeS ILP is orders of magnitude more efficient than the previous implementation - **Time Efficient !!!**





Modelling through multiple targets

Modelling of perturbation propagation from a receptor level
through hybrid interactions

Time course PHONEMeS

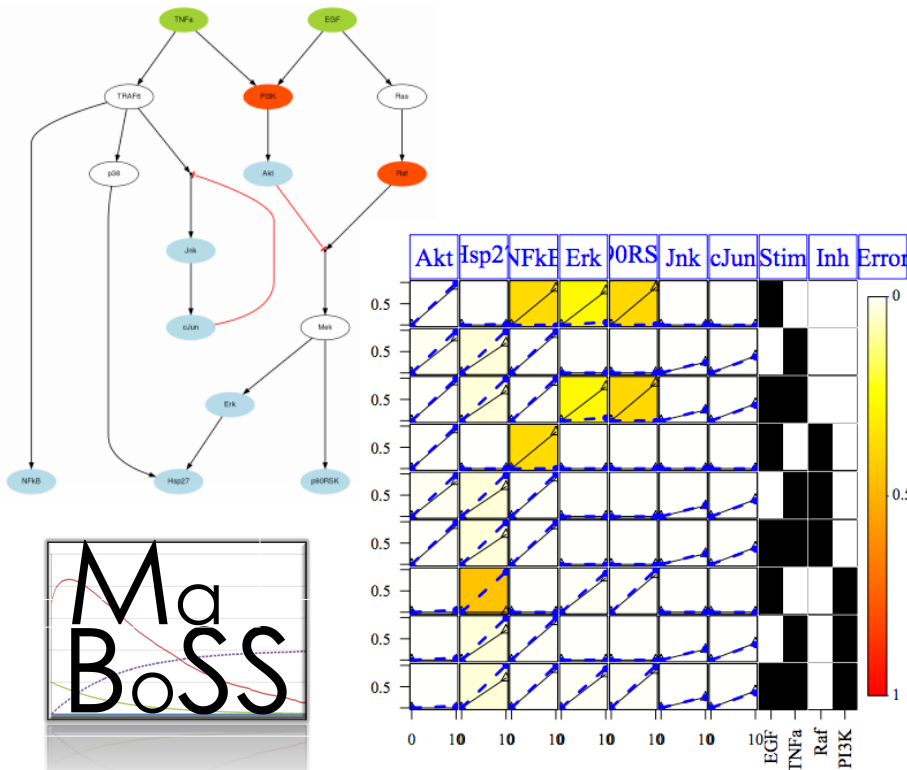


MaBoSS implementation in CellNOpt

MaBoSS, an algorithm for modelling biological networks in discrete framework with continuous time

Simulates the probabilities for each species to be active at each condition

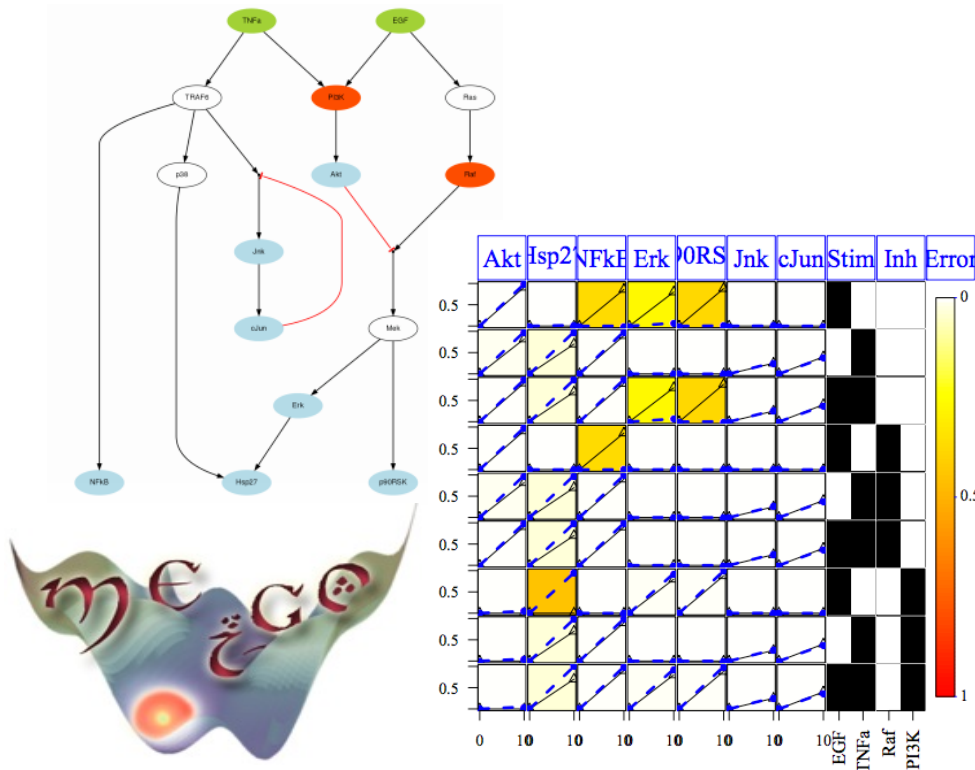
MaBoSS simulator for CellNOpt



Stoll et.al., *BMC Sys Biol*, 2012
C. Chevalier



New CNORode version released in *Github*



CNORode allows a quantitative description of a boolean model through the identification of logic ODE parameters

New features:

L1 regularisation penalty term is added to the objective function

An additional **steady state penalty** prioritises this parameter sets in which the steady state is reached

Bootstrap or optimisation with random resampling allows to determine the confidence intervals for each parameter

Download package in: <https://github.com/saezlab/CNORode2017>

see Eduati et al. Cancer Research 2017



Acknowledgements

Saez-Rodriguez group, specially:

Luis Tobalina

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Jakob Wirbel

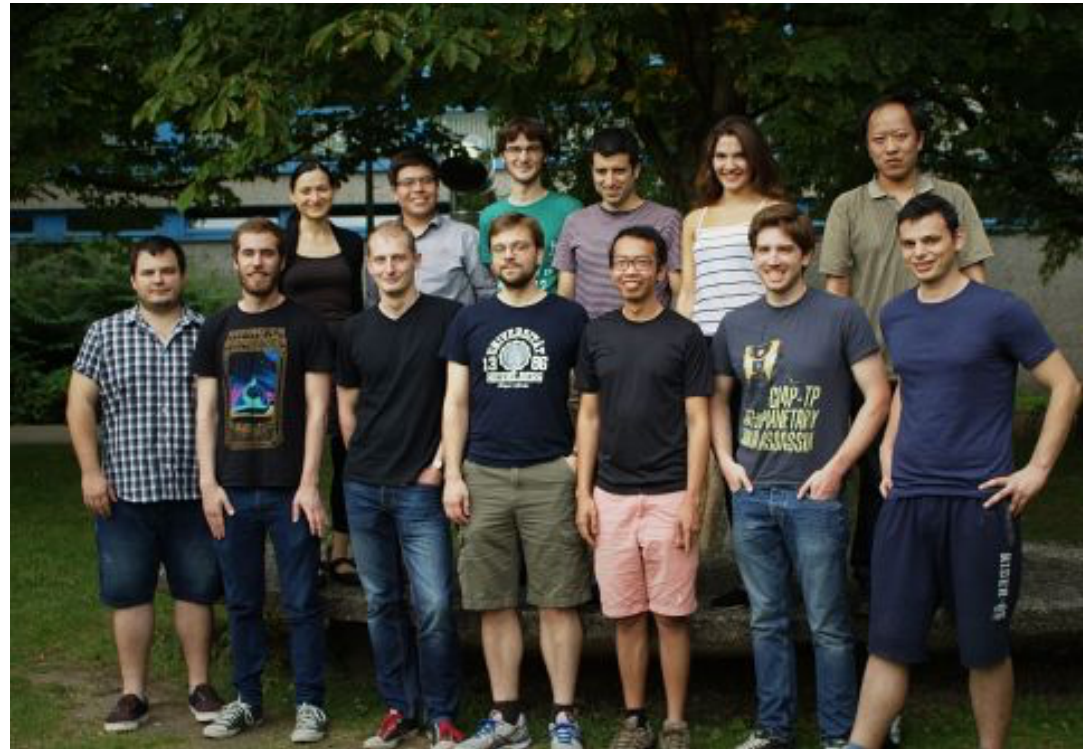
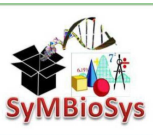
Attila Gabor

Celine Chevalier

Federica Eduati

Panuwat Trairatphisan

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Bioprocess Engineering Group
Vigo, Spain



Thank You

www.saezlab.org



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